# MATH GAPS: How to find them and fill them up!





# What is a math gap?

 A math learning gap refers to any math skill that a student should have previously mastered, but didn't.





# Why are math gaps a problem?





# The nature of math



#### Calculus

- Trigonometry
- Exponential Algebra
  - Geometry
  - Linear Algebra
    - Pre-Algebra
    - Arithmetic



# Where do we need multiplication?

- Factors/Greatest Common Factor
- Multiples/Least Common Multiple
- Common denominator
- Simplifying Fractions
- Equivalent Fractions
- Multiplying Fractions
- Dividing Fractions
- Measurement Conversions

- Roots
- Decimals
- Proportions
- Percents

Exponents and Square Roots





# What's Missing?

### Automaticity

Automaticity is the ability to deliver a correct answer immediately from memory without conscious thought, as opposed to relying on calculation.

- Stickney et al. (2012)



#### Automaticity

# Examples

- Instantly knowing that 7 + 8 = 15 without counting on fingers.
- Recognizing that **100** ÷ **25** = **4** immediately.

• Quickly recalling multiplication facts like  $6 \times 7 = 42$  without pausing.



# Why It Matters

- Helps with speed and efficiency in math tasks.
- Reduces frustration and mental fatigue.



# Frees up working memory for solving more complex problems.







Without automaticity in math facts and math fact families, it will be more difficult for students to engage in the higher order thinking skills that are necessary to solve many math problems.



# Where do math gaps occur?







### Skip counting

### Songs

# Which method works?

#### Stories

### Drills



# The research shows....



# **WORKS**

So find something your kids will enjoy!



# It's not the what, it's the HOW!





We need intentional, targeted practice to reinforce these foundations and fill the math gaps.





# To gain automaticity, take...



![](_page_17_Picture_2.jpeg)

![](_page_18_Picture_0.jpeg)

![](_page_18_Picture_1.jpeg)

![](_page_18_Picture_2.jpeg)

![](_page_18_Picture_3.jpeg)

![](_page_18_Picture_4.jpeg)

![](_page_18_Picture_6.jpeg)

![](_page_19_Picture_0.jpeg)

### **The Production Effect**

The dual action of speaking and hearing oneself has the most beneficial impact on long-term memory.

- The University of Waterloo

![](_page_19_Picture_4.jpeg)

![](_page_20_Picture_0.jpeg)

Speak it

![](_page_20_Picture_3.jpeg)

![](_page_20_Picture_4.jpeg)

![](_page_20_Picture_5.jpeg)

![](_page_20_Picture_6.jpeg)

![](_page_21_Picture_0.jpeg)

![](_page_22_Picture_0.jpeg)

Speak it

![](_page_22_Picture_3.jpeg)

# Dedicate Time

![](_page_22_Picture_5.jpeg)

![](_page_22_Picture_6.jpeg)

![](_page_22_Picture_93.jpeg)

![](_page_23_Picture_0.jpeg)

![](_page_23_Picture_1.jpeg)

![](_page_24_Picture_0.jpeg)

![](_page_25_Picture_0.jpeg)

Speak it

![](_page_25_Picture_3.jpeg)

# Dedicate Time

![](_page_25_Picture_5.jpeg)

**Easy Ones First** 

![](_page_25_Picture_7.jpeg)

![](_page_25_Picture_10.jpeg)

# **Recommended order for Teaching Addition Facts**

- Doubles (Dark Orange)
- Sums of 10 (Dark Green)
- 10 Plus (Dark Blue)
- Plus 0 (Dark Purple)

![](_page_26_Picture_5.jpeg)

## **Recommended order for Teaching Multiplication Facts**

- Times 0 (Dark Purple)
- Times 1 (Dark Purple)
- Times 2 (Dark Green)
- Times 10 (Dark Red)

Х
0
1
2
3
4
5
6
7
8
9
10

0	1	2	3	4	5	6	7	8	9	10
0	0	0	0	0	0	0	0	0	0	0
0	1	2	3	4	5	6	7	8	9	10
0	2	4	6	8	10	12	14	16	18	20
0	3	6	9	12	15	18	21	24	27	30
0	4	8	12	16	20	24	28	32	36	40
0	5	10	15	20	25	30	35	40	45	50
0	6	12	18	24	30	36	42	48	54	60
0	7	14	21	28	35	42	49	56	63	70
0	8	16	24	32	40	48	56	64	72	80
0	9	18	27	36	45	54	63	72	81	90
0	10	20	30	40	50	60	70	80	90	100

![](_page_27_Picture_7.jpeg)

![](_page_28_Picture_0.jpeg)

Speak it

![](_page_28_Picture_3.jpeg)

# Dedicate Time

![](_page_28_Picture_5.jpeg)

# **Easy Ones First**

![](_page_28_Picture_7.jpeg)

# Slow and Steady Wins the Race

![](_page_28_Picture_9.jpeg)

![](_page_29_Picture_0.jpeg)

# Teach three at a time

![](_page_29_Picture_2.jpeg)

# What's Missing?

### Automaticity

![](_page_30_Picture_2.jpeg)

![](_page_30_Picture_3.jpeg)

![](_page_31_Picture_0.jpeg)

![](_page_31_Picture_2.jpeg)

![](_page_31_Picture_3.jpeg)

![](_page_32_Picture_0.jpeg)

### Why It Matters

- Encourages deeper understanding rather than rote memorization.
- Allows students to approach problems in different ways. • Builds confidence in tackling unfamiliar problems.

![](_page_32_Picture_6.jpeg)

![](_page_33_Picture_0.jpeg)

### Examples

- Solving 63 29 by breaking it into parts:  $\circ$  (63 – 30) + 1 = 34 instead of traditional borrowing.
- Finding 16 × 25 by thinking:  $\circ$  16 × (100 ÷ 4) = (16 × 100) ÷ 4 = 1600 ÷ 4 = 400.
- Knowing that 12 x 15 can be found by:  $(12 \times 10) + (12 \times 5) = 120 + 60 = 180.$

![](_page_33_Picture_8.jpeg)

![](_page_34_Figure_0.jpeg)

overall math level

520-570

![](_page_35_Figure_0.jpeg)

# How do you fix gaps in

![](_page_36_Picture_1.jpeg)

![](_page_36_Picture_2.jpeg)

# Filling Pre-algebra gaps

Reteach

Find the gap

![](_page_37_Picture_3.jpeg)

### Do it in context

#### Practice

![](_page_37_Picture_6.jpeg)

 $5\frac{2}{4} - 2\frac{3}{5}$ 

![](_page_38_Picture_2.jpeg)

![](_page_39_Picture_2.jpeg)

	30	
$45\frac{2}{4} =$	<u>10</u> +20 20	Ste
<b>A</b> 3	12	Ste
$-2\frac{5}{5} =$	20	Ste
0	18	Ste
	20	Ste
2	$\frac{18}{20} \div \frac{2}{20} = \frac{9}{10}$	
	20 2 10	
$2 \frac{9}{10}$		

- ep 1: Find a common denominator
- ep 2: Make equivalent fractions
- ep 3: Regroup
- ep 4: Subtract mixed numbers
- ep 5: Simplify

![](_page_40_Picture_6.jpeg)

![](_page_41_Picture_1.jpeg)

		Saxon 5/4 or	Saxon 6/5 or	ng Algebra 2	Geometry	Advanced Math				
Торіс	Sub Topic	Intermediate 5	Intermediate 5	Course 1	Course 2	Course 3				
Time	Reading Time on a Clock on the 5 or 10 minute mark	х	Х	х	Х	Х	Х	Х	Х	х
Time	Reading Time on a Clock	Х	х	х	х	Х	Х	Х	Х	х
	Whole Numbers on a Number Line	Х	Х	Х	х	Х	Х	Х	Х	Х
Numbers P	Comparing Whole Numbers	Х	Х	х	Х	Х	Х	Х	Х	Х
Properties	Properties of Operations (Commutative, Distributive, Associative, Identity)				х	х	х	x	х	х
	Complete the Sequence		Х	Х	х	Х	Х	Х	Х	Х
Place Value	The Hundreds Place	х	Х	Х	х	Х	Х	Х	Х	Х
	Numbers up to 999	х	Х	х	х	Х	Х	Х	Х	х
	Numbers up to the Hundred Thousands		Х	Х	Х	Х	Х	Х	Х	Х
	Numbers up to the Hundred Millions		Х	Х	Х	Х	Х	Х	Х	Х
	Rounding Numbers to the Nearest Ten	Х	Х	х	Х	Х	Х	Х	Х	х
	Rounding Numbers to the Nearest Hundred		х	х	х	Х	Х	Х	Х	х
Dounding	Rounding Numbers to the Nearest Thousand		Х	Х	х	Х	Х	Х	Х	Х
Rounding	Rounding Numbers to the Nearest Million, Billion and Trillions			Х	Х	Х	Х	Х	Х	Х
	Estimating Addition and Subtraction Answers		Х	х	х	Х	Х	Х	Х	Х
	Estimating Multiplication and Division Answers		Х	х	х	Х	Х	Х	Х	Х
	Addition with Two Digits - No Regrouping	Х	Х	Х	Х	Х	Х	Х	Х	Х
	Addition with Two Digits - Some Regrouping	Х	Х	Х	Х	Х	Х	Х	Х	Х
Addition	Addition with Three Digits - No Regrouping	Х	Х	х	х	Х	Х	Х	Х	Х
	Addition with Three Digits - Some Regrouping	Х	Х	Х	х	Х	Х	Х	Х	х
	Addition with More Than Three Digits	Х	Х	х	Х	Х	Х	Х	Х	х
	Subtraction with Two Digits - No Regrouping	Х	Х	х	Х	Х	Х	Х	Х	х
	Subtraction with Two Digits - Some Regrouping	х	х	х	Х	Х	Х	Х	Х	х
Subtraction	Subtraction with Three Digits - No Regrouping	Х	Х	х	Х	Х	Х	Х	Х	х
subtraction	Subtraction with Three Digits - Some Regrouping	×	×	V	V	V	V	N/	N N	V

![](_page_42_Picture_0.jpeg)

![](_page_42_Picture_1.jpeg)

![](_page_42_Picture_3.jpeg)

# Should I change my math curriculum?

![](_page_43_Picture_1.jpeg)

![](_page_44_Picture_0.jpeg)

![](_page_44_Picture_1.jpeg)

![](_page_45_Picture_0.jpeg)

# **Rainbow Resource** Math Comparison Chart

#### MATH CURRICULUM COMPARISON CHART

MATH							Gra	des							Religious	Content	Pri	ice Ran	ige
Programs	РК	к	1	2	3	4	5	6	7	8	9	10	11	12	Christian	N/Secular	s	55	55
Saxon K-3 *		•	•	•	•											•			-
Saxon 3-12 *	$\vdash$			H		•	•	•		•		•	•	•		•		•	
Bob Jones	$\vdash$					•		•		•		•	•		•			$\square$	
AOP Horizons Math *	$\vdash$											$\square$				•		•	
AOP LIFEPAC Math *	$\vdash$														•			•	
AOP Monarch / Switched-On Schoolhouse	$\vdash$		-												•				
Math-U-See *												•			-	•			
Abeka Math													•		•			•	
Primary Math 2022 (Singapore)	-							-	-	-	-	-	-	-					
Primary Math (US) (Singangre) *	$\vdash$									H		$\vdash$							
Primary Math Standards Edition (SE) (Sinnanore) *	$\vdash$								$\vdash$	H		$\vdash$		$\vdash$					
Primary Math Common Core (CC) (Singapore)	$\vdash$							-		$\vdash$		$\vdash$	_			•		-	
Math in Forur / Cingapore) *	$\vdash$	-		-								H						-	
Column Hotes (Singapore)	$\vdash$	-		-	-	-	-	-	-	-			_					-	-
Evaluation with Mathematics (Analogia)	$\vdash$	-	-	÷			-	$\vdash$		$\vdash$		$\vdash$	_					-	
Good & Resultiful Simply Math	$\vdash$		-	-	-	-	-	$\vdash$		$\vdash$		$\vdash$							
Charling Matthe (Classings)	$\vdash$	-	-	-		-	-			$\vdash$		$\vdash$	_		· ·		-	$\vdash$	
Shaping Maths (Singapore)	$\vdash$		•	•	•	•	•	•								•			-
Christian Light Math			•	•	•	•	•	•	•	•	•	•	•	•	•			-	
Life of Fred			•	•	•	•	•	٠	•	•	•	•	•	•	•		•		
A+ Tutorsoft Math			•	•	•	•	•	•	•	•	•					•		•	
Starline Press Math					•	•	•	•	•	•	•	•	•	•		•		$\square$	
ShillerMath	٠	٠	•	•	٠	٠	٠	٠	٠							•		•	
enVision Math (2017/2018)		•	٠	•	٠	•	•	٠	٠	٠	•	٠	٠			•		$\square$	-
Purposeful Design Math (2nd Ed.)		•	٠	•	٠	٠	٠	٠							•				-
Making Math Meaningful		٠	٠	٠	٠	٠	٠	٠	٠	٠					•		•		
RightStart Mathematics *		•	٠	•	٠	•	٠	٠	٠							•			_
MCP Mathematics		٠	٠	•	٠	٠	٠	٠								•	•		
Conventional (Spunky Donkey) / Study Time Math			٠	•	٠	٠	٠	٠	٠	•					•		•		
Liberty Mathematics		٠	٠	•											•		٠		
Miquon Math			٠	•	٠											•	•		
Math Mammoth (Light Blue series) *			٠	•	٠	٠	٠	٠	٠							•	•		
Ray's Arithmetic			٠	•	٠	•	•	٠	•	٠						•	•		
Ray's for Today			٠	•	٠	٠	٠	٠	٠	٠						•		•	
Rod & Staff Mathematics			٠	•	٠	٠	٠	٠	•	٠					•		•		
Jump Math			٠	•	٠	٠	٠	٠	•	٠						•	٠		
ThemeVille Math*			٠	٠	٠	٠	٠									•		•	
Beast Academy (from Art of Problem Solving) *				٠	٠	٠	٠									•			•
Strayer-Upton Practical Arithmetic					•	•	•	٠	•	٠						•	•		
Art of Problem Solving *								٠	٠	٠	٠	٠	٠	٠		•		•	
Paradigm Accelerated									٠	٠						•		•	
Principles of Mathematics/Algebra 2									٠	٠			•	٠	•			٠	
A Fresh Approach										٠	٠	٠	٠	٠		•		٠	
Jacobs Math											٠	٠				•			•
Foerster Math (Math Without Borders)											٠	٠	•	٠		•			•
VideoText										٠	٠	٠	•	٠		•			•
Math Lessons for a Living Education		٠	٠	٠	٠	٠	٠	٠							•		•		
Mathematical Reasoning	٠	٠	٠	٠	٠	٠	٠	٠	٠	٠	٠	٠				•	•		
Developmental Math			•	•	•	•	٠	٠	•	٠						•	•		
Math Power Basics								•	•	•	•	•	•	•		•	•		
			_		_		_		_		_								

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	Appro	oach	M	anip <u>ulati</u>	ves	Teacher Involvement		COSS					
Spiral	Sequential	Conceptual/Topical	Reg	Opt	RRC kit	Low	Med	High	High	High	High	Aligned	Notes
•			•		•			•		Scripted teacher manuals.			
•				•		•				Teaching tutorials available separately.			
•								•		Paper manipulatives included.			
•				•	•		•			Grades 4-8 contain some religious content.			
	•						•						
	•					•				Monarch is online only. SOS is computer-base			
	•		•				•			Mastery-based. Optional songs some Christian cor			
•			•				•						
	•		•				•			Digital manipulatives. Online components.			
	•			•			•						
	•			•			•			Aligned to 1997 CA Standards. 2008 Ed.			
	•			•			•		•				
	•		•		•		•		•				
	•			•			•						
	•			•				•		Projects included with each lesson.			
•			•				•			K-3: parent taught & includes manipulatives: AK o			
-	•		-							2013. Sincaporean money Metric Online compone			
				-					-	Suggested manipulatives for lower grades			
							-	<u> </u>		Brief Christian references in elementary level			
							<u> </u>			Computer based			
									<u> </u>	competer-based.			
				<u> </u>		-			<u> </u>	Discourse Montescol scoresch			
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	· ·			· ·					<u> </u>	E-book option for teacher educit.			
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	<u> </u>							<u> </u>	<u> </u>	Modified Sequential.			
•							<u> </u>	<u> </u>		Concurrable workbasiz			
	· ·			<u> </u>		•			<u> </u>	Consumable workbooks.			
		•	•					•	<u> </u>	Uses Cuisenaire rods.			
	•			•		•				B & W or color versions available.			
	•						•	<u> </u>	<u> </u>				
	•			•			•	<u> </u>	<u> </u>				
	•						•						
	•			<u> </u>				•	•				
•			•		<u> </u>		•		<u> </u>	Manipulatives used at all levels.			
	<u> </u>	•		<u> </u>		•	<u> </u>	<u> </u>	<u> </u>	Recommended for gifted students.			
	•						•			No Teacher Guide.			
	•					•				Recommended for gifted students.			
	•					•							
	•					•							
	•					•							
	•					•				Teaching tutorials available separately.			
	•					•				MWB Teaching tutorials available separately.			
	•					•				DVD or online format.			
		•	•					•		Extra practice (L1-3). Teaching Companion av			
•						•							
	•			•		•				Skill-based levels.			

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![](_page_45_Picture_9.jpeg)

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![](_page_46_Picture_1.jpeg)

![](_page_46_Picture_3.jpeg)

![](_page_47_Picture_0.jpeg)

![](_page_47_Picture_1.jpeg)

![](_page_48_Picture_0.jpeg)

![](_page_48_Picture_1.jpeg)

![](_page_49_Picture_0.jpeg)

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 Learn Multiplication & Division Facts in 90 days

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![](_page_50_Picture_3.jpeg)

![](_page_50_Picture_4.jpeg)

![](_page_51_Picture_0.jpeg)

![](_page_52_Picture_0.jpeg)

![](_page_52_Picture_1.jpeg)